# Meanings as Proposals: an Inquisitive Approach to Exhaustivity 

Matthijs Westera

Institute for Logic, Language and Computation University of Amsterdam

Genève, ICL, July $26^{\text {th }} 2013$

# Meanings as Proposals: an Inquisitive Approach to Exhaustivity 

Matthijs Westera

Institute for Logic, Language and Computation University of Amsterdam

Genève, ICL, July $26^{\text {th }} 2013$

# Meanings as Proposals: an Inquisitive Approach to Exhaustivity Attentive 

Matthijs Westera

Institute for Logic, Language and Computation University of Amsterdam

Genève, ICL, July $26^{\text {th }} 2013$

# Aheanings as Proposals: an Inquisitive Approach to Exhaustivity Attentive 

Matthijs Westera

Institute for Logic, Language and Computation University of Amsterdam

Genève, ICL, July $26^{\text {th }} 2013$

# Long live Grice! Aheanings as Proposals: an Inquisitive Approach to Exhaustivity Attentive 

Matthijs Westera

Institute for Logic, Language and Computation University of Amsterdam

Genève, ICL, July $26^{\text {th }} 2013$

## Goal of this talk

(1) Which colours (among red, green and blue) does John like? He likes blue. $\quad \sim$ He doesn't like red, green.

## Goal of this talk

(1) Which colours (among red, green and blue) does John like? He likes blue. $\sim$ He doesn't like red, green.

Conversational implicature (Grice, 1975)
An implicature, the supposition of which is necessary for maintaining the assumption that the speaker is cooperative.

## Goal of this talk

(1) Which colours (among red, green and blue) does John like? He likes blue.
$\leadsto$ He doesn't like red, green.
Conversational implicature (Grice, 1975)
An implicature, the supposition of which is necessary for maintaining the assumption that the speaker is cooperative.

1. Had sp. believed John likes red, she should have said so.

## Goal of this talk

(1) Which colours (among red, green and blue) does John like? He likes blue.
$\leadsto$ He doesn't like red, green.

## Conversational implicature (Grice, 1975)

An implicature, the supposition of which is necessary for maintaining the assumption that the speaker is cooperative.

1. Had sp. believed John likes red, she should have said so.
2. She doesn't believe that he likes red.

## Goal of this talk

(1) Which colours (among red, green and blue) does John like? He likes blue. $\leadsto$ He doesn't like red, green.

## Conversational implicature (Grice, 1975)

An implicature, the supposition of which is necessary for maintaining the assumption that the speaker is cooperative.

1. Had sp. believed John likes red, she should have said so.
2. She doesn't believe that he likes red.
3. She believes that he doesn't like red.

## Goal of this talk

(1) Which colours (among red, green and blue) does John like? He likes blue.
$\leadsto$ He doesn't like red, green.

## Conversational implicature (Grice, 1975)

An implicature, the supposition of which is necessary for maintaining the assumption that the speaker is cooperative.

1. Had sp. believed John likes red, she should have said so.
2. She doesn't believe that he likes red.
... ('the epistemic step' - Sauerland, 2004)
3. She believes that he doesn't like red.

## Goal of this talk

(1) Which colours (among red, green and blue) does John like? He likes blue.
$\leadsto$ He doesn't like red, green.

## Conversational implicature (Grice, 1975)

An implicature, the supposition of which is necessary for maintaining the assumption that the speaker is cooperative.

1. Had sp. believed John likes red, she should have said so.
2. She doesn't believe that he likes red.
... ('the epistemic step' - Sauerland, 2004)
3. She believes that he doesn't like red.
"[the epistemic] step does not follow from
Gricean maxims and logic alone." - Chierchia, et al. (2008)

## Goal of this talk

(1) Which colours (among red, green and blue) does John like? He likes blue. $\leadsto$ He doesn't like red, green.

## Conversational implicature (Grice, 1975)

An implicature, the supposition of which is necessary for maintaining the assumption that the speaker is cooperative.

1. Had sp. believed John likes red, she should have said so.
2. She doesn't believe that he likes red.
... ('the epistemic step' - Sauerland, 2004)
3. She believes that he doesn't like red.
"[the epistemic] step does not follow from
Gicean maxims and logic alone." - Chierchia, et al. (2008)
Wrong, it does!

## Outline

1. Diagnosis
2. Solution
3. Conclusion
4. Related concepts and puzzles

## 1. Diagnosis

(2) a. Which colours (among red, green and blue) does John like?
b. He likes blue.
$\leadsto$ He doesn't like red
c. He likes blue, or blue and red. $\nrightarrow$ He doesn't like red

## 1. Diagnosis

(2) a. Which colours (among red, green and blue) does John like?
b. He likes blue.
$\leadsto$ He doesn't like red
c. He likes blue, or blue and red. $\nrightarrow \mathrm{He}$ doesn't like red

## Intuition

(2b) and (2c) differ in their attentive content.

## 1. Diagnosis

(2) a. Which colours (among red, green and blue) does John like?
b. He likes blue. $\leadsto$ He doesn't like red
c. He likes blue, or blue and red. $\nrightarrow$ He doesn't like red

## Intuition

(2b) and (2c) differ in their attentive content.

- (2c) draws attention to the poss. that John likes blue and red.


## 1. Diagnosis

(2) a. Which colours (among red, green and blue) does John like?
b. He likes blue. $\leadsto$ He doesn't like red
c. He likes blue, or blue and red. $\nrightarrow$ He doesn't like red

## Intuition

(2b) and (2c) differ in their attentive content.

- (2c) draws attention to the poss. that John likes blue and red.
- (And so does (2a).)


## 1. Diagnosis

(2) a. Which colours (among red, green and blue) does John like?
b. He likes blue.
c. He likes blue, or blue and red.
$\leadsto$ He doesn't like red $\psi$ He doesn't like red

## Intuition

(2b) and (2c) differ in their attentive content.

- (2c) draws attention to the poss. that John likes blue and red.
- (And so does (2a).)
- (2b) doesn't; it leaves the possibility unattended.


## 1. Diagnosis

(2) a. Which colours (among red, green and blue) does John like?
b. He likes blue.
c. He likes blue, or blue and red.
$\leadsto$ He doesn't like red
to He doesn't like red

## Intuition

(2b) and (2c) differ in their attentive content.

- (2c) draws attention to the poss. that John likes blue and red.
- (And so does (2a).)
- (2b) doesn't; it leaves the possibility unattended.

Apparently, pragmatic reasoning is sensitive to this.

## 1. Diagnosis

(2) a. Which colours (among red, green and blue) does John like?
b. He likes blue.
c. He likes blue, or blue and red.
$\leadsto$ He doesn't like red to He doesn't like red

## Intuition

(2b) and (2c) differ in their ttentive content.

- (2c) draws attention to the poss. that John likes blue and red.
- (And so does (2a).)
- (2b) doesn't; it leaves the possibility unattended.

Apparently, pragmatic reasoning is sensitive to this.

## 1. Diagnosis

(2) a. Which colours (among red, green and blue) does John like?
b. He likes blue.
c. He likes blue, or blue and red.
$\leadsto$ He doesn't like red to He doesn't like red

## Intuition

(2b) and (2c) differ in their ttentive content.

- (2c) draws attention to the poss. that John likes blue and red.
- (And so does (2a).)
- (2b) doesn't; it leaves the possibility unattended.

Apparently, pragmatic reasoning is sensitive to this.

## 1. Diagnosis

(2) a. Which colours (among red, green and blue) does John like?
b. He likes blue.
c. He likes blue, or blue and red.
$\leadsto$ He doesn't like red to He doesn't like red

Intuition a richer
(2b) and (2c) differ in their ttentive content. semantics

- (2c) draws attention to the poss. that John likes blue and red.
- (And so does (2a).)
- (2b) doesn't; it leaves the possibility unattended.

Apparently, pragmatic reasoning is sensitive to this.

## 1. Diagnosis

(2) a. Which colours (among red, green and blue) does John like?
b. He likes blue.
c. He likes blue, or blue and red.
$\leadsto$ He doesn't like red
to He doesn't like red

Intuition
(2b) and (2c) differ in their ttentive content. a richer

- (2c) draws attention to the poss. that John likes blue and red.
- (And so does (2a).)
- (2b) doesn't; it leaves the possibility unattended.

Apparently, pragmatic reasoning is sensitive to this. maxim of Relation

## 2. Solution

2.1. Translation into logic
2.2. Semantics
2.3. Pragmatics
2.4. Predictions

### 2.1. Translation into logic

(3) a. Which colours (among red, green and blue) does John like?
b. He likes blue.
c. He likes blue, or blue and red.
$\leadsto$ He doesn't like red
$\nrightarrow$ He doesn't like red

### 2.1. Translation into logic

(3) a. Which colours (among red and blue) does John like?
b. He likes blue.
c. He likes blue, or blue and red.
$\leadsto$ He doesn't like red
$\nrightarrow$ He doesn't like red

### 2.1. Translation into logic

(3) a. There are colours (among red and blue) that John likes.
b. He likes blue.
c. He likes blue, or blue and red.
$\leadsto$ He doesn't like red
$\nrightarrow$ He doesn't like red

### 2.1. Translation into logic

(3) a. John likes blue, red, or blue and red.
b. He likes blue.
c. He likes blue, or blue and red.
$\leadsto$ He doesn't like red
$\nrightarrow$ He doesn't like red

### 2.1. Translation into logic

(3) a. John likes blue, red, or blue and red.

$$
p \vee q \vee(p \wedge q)
$$

b. He likes blue.

$$
\begin{array}{r}
p \\
p \vee(p \wedge q)
\end{array}
$$

c. He likes blue, or blue and red.
2.2. Semantics (Roelofsen, 2011)

### 2.2. Semantics (Roelofsen, 2011)

- Possibility: a set of worlds $(a, b)$


### 2.2. Semantics (Roelofsen, 2011)

- Possibility: a set of worlds $(a, b)$
- Proposition: a set of possibilities $(A, B,[\varphi])$


### 2.2. Semantics (Roelofsen, 2011)

- Possibility: a set of worlds $(a, b)$
- Proposition: a set of possibilities $(A, B,[\varphi])$
- Informative content: $|\varphi|:=\bigcup[\varphi]$


### 2.2. Semantics (Roelofsen, 2011)

- Possibility: a set of worlds $(a, b)$
- Proposition: a set of possibilities $(A, B,[\varphi])$
- Informative content: $|\varphi|:=\bigcup[\varphi]$
(3a) $[p \vee q \vee(p \wedge q)]$
(3b) $[p]$
(3c) $[p \vee(p \wedge q)]$
2.2. Semantics (Roelofsen, 2011)
- Possibility: a set of worlds $(a, b)$
- Proposition: a set of possibilities $(A, B,[\varphi])$
- Informative content: $|\varphi|:=\bigcup[\varphi]$

(3a) $[p \vee q \vee(p \wedge q)]$
(3b) $[p]$

(3c) $[p \vee(p \wedge q)]$
2.2. Semantics (Roelofsen, 2011)
- Possibility: a set of worlds $(a, b)$
- Proposition: a set of possibilities $(A, B,[\varphi])$
- Informative content: $|\varphi|:=\bigcup[\varphi]$

(3a) $[p \vee q \vee(p \wedge q)]$
(3b) $[p]$
(3c) $[p \vee(p \wedge q)]$
Entailment
$A$ entails $B, A \vDash B$, iff
(i) $\cup A \subseteq \cup B$; and
(ii) for all $b \in B$, if $b \cap \cup A \neq \varnothing, b \cap \cup A \in A$
2.2. Semantics (Roelofsen, 2011)
- Possibility: a set of worlds $(a, b)$
- Proposition: a set of possibilities $(A, B,[\varphi])$
- Informative content: $|\varphi|:=\bigcup[\varphi]$

(3a) $[p \vee q \vee(p \wedge q)]$
Entailment
$A$ entails $B, A \vDash B$, iff
(i) $\cup A \subseteq \cup B$; and $\longrightarrow$ at least as informative
(ii) for all $b \in B$, if $b \cap \cup A \neq \varnothing, b \cap \cup A \in A$
2.2. Semantics (Roelofsen, 2011)
- Possibility: a set of worlds $(a, b)$
- Proposition: a set of possibilities $(A, B,[\varphi])$
- Informative content: $|\varphi|:=\bigcup[\varphi]$

(3a) $[p \vee q \vee(p \wedge q)]$
Entailment
$A$ entails $B, A \vDash B$, iff
(i) $\cup A \subseteq \cup B$; and
$\longrightarrow$ at least as informative
(ii) for all $b \in B$, if $b \cap \cup A \neq \varnothing, b \cap \cup A \in A$
2.2. Semantics (Roelofsen, 2011)
- Possibility: a set of worlds $(a, b)$
- Proposition: a set of possibilities $(A, B,[\varphi])$
- Informative content: $|\varphi|:=\bigcup[\varphi]$

(3a) $[p \vee q \vee(p \wedge q)]$
Entailment
$A$ entails $B, A \vDash B$, iff
(i) $\cup A \subseteq \cup B$; and
$\longrightarrow$ at least as informative
(ii) for all $b \in B$, if $b \cap \cup A \neq \varnothing, b \cap \cup A \in A$


Now, (3c) $\vDash(3 a)$, but (3b) $\neq(3 a)$.
2.3. Pragmatics

The relevant maxims

1. Quality:
2. Quantity:
3. Relation:

### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality:
2. Quantity:
3. Relation:

### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity:
3. Relation:

### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation:

### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation: $\{r \cap s \mid r \in R\} \vDash Q$.

### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation: $\{r \cap s \mid r \in R\} \vDash Q$.
(4) Did John go to the party?

It was raining.

### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation: $\{r \cap s \mid r \in R\} \vDash Q$.
(4) Did John go to the party? It was raining.


### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation: $\{r \cap s \mid r \in R\} \vDash Q$.
(4) Did John go to the party? It was raining.

2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation: $\{r \cap s \mid r \in R\} \vDash Q$.
(4) Did John go to the party? It was raining.


### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation: $\{r \cap s \mid r \in R\} \vDash Q$.
(4) Did John go to the party? It was raining.


### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation: $\{r \cap s \mid r \in R\} \vDash Q$.
(4) Did John go to the party? It was raining.


### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation: $\{r \cap s \mid r \in R\} \vDash Q$.
(4) Did John go to the party? It was raining. $\leadsto$ If it rained, John \{did / didn't \} go.


### 2.3. Pragmatics

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation: $\{r \cap s \mid r \in R\} \vDash Q$.

### 2.3. Pragmatics

(cf. Groenendijk and Stokhof, 1984; Roberts, 1996; Spector, 2007)

The relevant maxims
For a cooperative speaker with information $s$, responding $R$ to $Q$ :

1. Quality: $s \subseteq \cup R$.
2. Quantity: For all $Q^{\prime} \subseteq Q$, if $s \subseteq \cup Q^{\prime}$ then $\cup R \subseteq \cup Q^{\prime}$.
3. Relation: $\{r \cap s \mid r \in R\} \vDash Q$.

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$ 1. $s \subseteq|p \vee(p \wedge q)|$

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$ 1. $s \subseteq|p \vee(p \wedge q)|=|p|$

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. (p)
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

1. $s \subseteq|p \vee(p \wedge q)|=|p|$
(Quality)
2. $s \nsubseteq|q|$
(Quantity)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$ b. He likes blue. ( $p$ )
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

1. $s \subseteq|p \vee(p \wedge q)|=|p|$
(Quality)
2. $s \nsubseteq|q|$

$$
p \vee(p \wedge q) \vDash p \vee q \vee(p \wedge q)
$$

(Quantity)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$ b. He likes blue. (p)
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

1. $s \subseteq|p \vee(p \wedge q)|=|p|$
2. $s \nsubseteq|q|$
3.     - 

$$
p \vee(p \wedge q] \vDash p \vee q \vee(p \wedge q)
$$

(Quality)
(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. (p)

1. $s \subseteq|p|$
(Quality)
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

$$
\begin{aligned}
& \text { 1. } s \subseteq|p \vee(p \wedge q)|=|p| \\
& \text { 2. } s \neq|q| \\
& \text { 3. - } p \vee(p \wedge q] \vDash p \vee q \vee(p \wedge q)
\end{aligned}
$$

(Quality)
(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. (p)

$$
\begin{aligned}
& \text { 1. } s \subseteq|p| \\
& \text { 2. } s \nsubseteq|q|
\end{aligned}
$$

(Quality)
(Quantity)
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

$$
\begin{aligned}
& \text { 1. } s \subseteq|p \vee(p \wedge q)|=|p| \\
& \text { 2. } s \nsubseteq|q| \\
& \text { 3. - } p \vee(p \wedge q) \vDash p \vee q \vee(p \wedge q)
\end{aligned}
$$

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. (p)

1. $s \subseteq|p|$
2. $s \nsubseteq|q|$
$p \stackrel{!!!}{\nvdash} p \vee q \vee(p \wedge q)$
(Quality)
(Quantity)
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

$$
\begin{aligned}
& \text { 1. } s \subseteq|p \vee(p \wedge q)|=|p| \\
& \text { 2. } s \nsubseteq|q| \\
& \text { 3. - } p \vee(p \wedge q) \vDash p \vee q \vee(p \wedge q)
\end{aligned}
$$

(Quality)
(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )

1. $s \subseteq|p|$
2. $s \nsubseteq|q|$
$p \stackrel{!!!}{\nvdash} p \vee q \vee[p \wedge q]$
(Quality)
(Quantity)

c. He likes blue, or blue and red. $(p \vee(p \wedge q))$
3. $s \subseteq|p \vee(p \wedge q)|=|p|$
(Quality)
4. $s \nsubseteq|q|$
5.     - 

$$
p \vee(p \wedge q] \vDash p \vee q \vee[p \wedge q]
$$

(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )

1. $s \subseteq|p|$
2. $s \nRightarrow|q|$
$p \nLeftarrow!!!p \vee q \vee(p \wedge q)$
(Quality)
(Quantity)

c. He likes blue, or blue and red. $(p \vee(p \wedge q))$
3. $s \subseteq|p \vee(p \wedge q)|=|p|$
(Quality)
4. $s \nsubseteq|q|$
5.     - 

$$
p \vee(p \wedge q] \vDash p \vee q \vee[p \wedge q]
$$

(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )

1. $s \subseteq|p|$
2. $s \nsubseteq|q|$
$p \nLeftarrow!!!$
(Quality)
(Quantity)

c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

$$
\begin{aligned}
& \text { 1. } s \subseteq|p \vee(p \wedge q)|=|p| \\
& \text { 2. } s \notin|q| \\
& \text { 3. - } p \vee(p \wedge q) \vDash p \vee q \vee(p \wedge q)
\end{aligned}
$$

(Quality)
(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )

1. $s \subseteq|p|$
2. $s \nRightarrow|q|$
$p \nLeftarrow!!!$
(Quality)
(Quantity)

c. He likes blue, or blue and red. $(p \vee(p \wedge q))$
3. $s \subseteq|p \vee(p \wedge q)|=|p|$
(Quality)
4. $s \nsubseteq|q|$
5.     - 

$$
p \vee(p \wedge q] \vDash p \vee q \vee(p \wedge q)
$$

(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )

1. $s \subseteq|p|$
2. $s \nsubseteq|q|$
$p \stackrel{!!!}{\nvdash} p \vee q \vee[p \wedge q]$
(Quality)
(Quantity)

c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

$$
\begin{aligned}
& \text { 1. } s \subseteq|p \vee(p \wedge q)|=|p| \\
& \text { 2. } s \notin|q| \\
& \text { 3. - } p \vee(p \wedge q) \vDash p \vee q \vee(p \wedge q)
\end{aligned}
$$

(Quality)
(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )

1. $s \subseteq|p|$
2. $s \nsubseteq|q|$
3. $\left.s \subseteq\left|\frac{\prime!!}{|p|} \cup\right| q \right\rvert\,$ or $s \subseteq \overline{|p|} \cup \overline{|q|} p \vee q \vee(p \wedge q)$
(Quality)
(Quantity)
(Relation)
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

$$
\begin{aligned}
& \text { 1. } s \subseteq|p \vee(p \wedge q)|=|p| \\
& \text { 2. } s \neq|q| \\
& \text { 3. - } p \vee(p \wedge q] \vDash p \vee q \vee(p \wedge q)
\end{aligned}
$$

(Quality)
(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )

$$
\begin{aligned}
& \text { 1. } s \subseteq|p| \\
& \text { 2. } s \nsubseteq|q| \\
& \text { 3. } \left.s \subseteq\left|\frac{1!!}{|p|} \cup\right| q \right\rvert\, \text { or } s \subseteq \overline{|p|} \cup \overline{|q|}
\end{aligned}
$$

(Quality)
(Quantity)
(Relation)
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

$$
\begin{aligned}
& \text { 1. } s \subseteq|p \vee(p \wedge q)|=|p| \\
& \text { 2. } s \neq|q| \\
& \text { 3. - } p \vee(p \wedge q) \vDash p \vee q \vee(p \wedge q)
\end{aligned}
$$

(Quality)
(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. (p)

1. $s \subseteq|p|$
2. $s \nsubseteq|q|$
$p \nmid!!!$
$\cup \mid q \vee$
$|q|$
3. $s \subseteq \overline{|p|} \cup|q|$ or $s \subseteq \overline{|p|} \cup \overline{|q|}$
4. $s \subseteq \overline{|q|}$
(Quality)
(Quantity)
(Relation)
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

$$
\begin{aligned}
& \text { 1. } s \subseteq|p \vee(p \wedge q)|=|p| \\
& \text { 2. } s \nsubseteq|q| \\
& \text { 3. - } p \vee(p \wedge q) \vDash p \vee q \vee(p \wedge q)
\end{aligned}
$$

(Quality)
(Quantity)
(Relation)

### 2.4. Predictions

(3) a. John likes blue, red, or blue and red. $(p \vee q \vee(p \wedge q))$
b. He likes blue. ( $p$ )

(Quality)
(Quantity)
(Relation)
4. $s \subseteq|9|$ exhaustivity!
c. He likes blue, or blue and red. $(p \vee(p \wedge q))$

$$
\begin{aligned}
& \text { 1. } s \subseteq|p \vee(p \wedge q)|=|p| \\
& \text { 2. } s \nsubseteq|q| \\
& \text { 3. - } p \vee(p \wedge q) \vDash p \vee q \vee(p \wedge q)
\end{aligned}
$$

(Quality)
(Quantity)
(Relation)

## 3. Conclusion

Main finding:

## 3. Conclusion

Main finding:

- If we feed the maxims attentive content


## 3. Conclusion

Main finding:

- If we feed the maxims attentive content
-     - which we must anyway, to distinguish between (3b,3c) -


## 3. Conclusion

Main finding:

- If we feed the maxims attentive content
-     - which we must anyway, to distinguish between (3b,3c) -
- then the epistemic step follows from the cooperative principle.


## 3. Conclusion

Main finding:

- If we feed the maxims attentive content
-     - which we must anyway, to distinguish between (3b,3c) -
- then the epistemic step follows from the cooperative principle.

Take-home messages:

- Pragmatic reasoning is sensitive to attentive content.
- Exhaustivity implicatures are conversational implicatures.


## 4. Related concepts and puzzles

4.1. The opinionatedness assumption
4.2. 'Alternatives'
4.3. 'Embedded' implicatures
4.4. Other suitable semantics
4.5. Roberts's (1996) 'relevance'
4.6. One-sided/two-sided numerals

### 4.1. The opinionatedness assumption

Most existing work (Sauerland, 2004):

### 4.1. The opinionatedness assumption

Most existing work (Sauerland, 2004):

1. The speaker doesn't believe $q$

### 4.1. The opinionatedness assumption

Most existing work (Sauerland, 2004):

1. The speaker doesn't believe $q$
2. She believes either $q$ or $\neg q$
(Quantity)
(Context)

### 4.1. The opinionatedness assumption

Most existing work (Sauerland, 2004):

1. The speaker doesn't believe $q$
2. She believes either $q$ or $\neg q$
(Quantity)
(Context)
3. She believes $\neg q$

### 4.1. The opinionatedness assumption

Most existing work (Sauerland, 2004):

1. The speaker doesn't believe $q$
2. She believes either $q$ or $\neg q$
3. She believes $\neg q$

### 4.1. The opinionatedness assumption

Most existing work (Sauerland, 2004):

1. The speaker doesn't believe $q$
2. She believes either $q$ or $\neg q$
3. She believes $\neg q$

Counterexample:
(5) I'm asking the wrong person, but which colours does J. like? He likes blue. $\leadsto$ He doesn't like red.

### 4.1. The opinionatedness assumption

Most existing work (Sauerland, 2004):

1. The speaker doesn't believe $q$
2. She believes either $q$ or $\neg q$
3. She believes $\neg q$

Counterexample:
(5) I'm asking the wrong person, but which colours does J. like? He likes blue. $\leadsto$ He doesn't like red.

Instead, in my approach:

- Opinionatedness follows from Quality + Relation implicatures


## 4.2. 'Alternatives'

Existing approaches (since Gazdar, 1979?):

- 'Why did the speaker not say " $p \wedge q$ "?'


## 4.2. 'Alternatives'

Existing approaches (since Gazdar, 1979?):

- 'Why did the speaker not say " $p \wedge q$ " ?'
- Mere ignorance is sufficient reason.


## 4.2. 'Alternatives'

Existing approaches (since Gazdar, 1979?):

- 'Why did the speaker not say " $p \wedge q$ " ?'
- Mere ignorance is sufficient reason.

My approach:

- 'Why did the speaker not say " $p \vee(p \wedge q)$ " ?'


## 4.2. 'Alternatives'

Existing approaches (since Gazdar, 1979?):

- 'Why did the speaker not say " $p \wedge q$ " ?'
- Mere ignorance is sufficient reason.

My approach:

- 'Why did the speaker not say " $p \vee(p \wedge q)$ "?'
- Ignorance is no excuse.


## 4.2. 'Alternatives'

Existing approaches (since Gazdar, 1979?):

- 'Why did the speaker not say " $p \wedge q$ " ?'
- Mere ignorance is sufficient reason.

My approach:

- 'Why did the speaker not say " $p \vee(p \wedge q)$ "?'
- Ignorance is no excuse.
- Hence something stronger is implied: exhaustivity.


## 4.2. 'Alternatives'

Existing approaches (since Gazdar, 1979?):

- 'Why did the speaker not say " $p \wedge q$ "?'
- Mere ignorance is sufficient reason.

My approach:

- 'Why did the speaker not say " $p \vee(p \wedge q)$ "?'
- Ignorance is no excuse.
- Hence something stronger is implied: exhaustivity.

More take-home messages

- The 'alternatives' are fully determined by the maxims.
- Speakers need not reason in terms of alternatives.


## 4.3. 'Embedded' implicatures

Chierchia, et al. (2008), and much subsequent discussion
(6) Which books (among O. and K.L.) did every student read? Every student read O. or K.L. $\leadsto$ No student read both.

## 4.3. 'Embedded' implicatures

Chierchia, et al. (2008), and much subsequent discussion
(6) Which books (among O. and K.L.) did every student read? Every student read O. or K.L. $\sim$ No student read both.

The problem
The problem has never been the Gricean approach as such, but rather to find the right 'alternatives'.

## 4.3. 'Embedded' implicatures

Chierchia, et al. (2008), and much subsequent discussion
(6) Which books (among O. and K.L.) did every student read? Every student read O. or K.L. $\sim$ No student read both.

The problem
The problem has never been the Gricean approach as such, but rather to find the right 'alternatives'.

In the present theory:

- The maxims are sensitive to attentive content


## 4.3. 'Embedded' implicatures

Chierchia, et al. (2008), and much subsequent discussion
(6) Which books (among O. and K.L.) did every student read? Every student read O. or K.L. $\sim$ No student read both.

The problem
The problem has never been the Gricean approach as such, but rather to find the right 'alternatives'.

In the present theory:

- The maxims are sensitive to attentive content
- Attentive content mirrors sub-sentential structure.


## 4.3. 'Embedded' implicatures

Chierchia, et al. (2008), and much subsequent discussion
(6) Which books (among O. and K.L.) did every student read? Every student read O. or K.L. $\leadsto$ No student read both.

The problem
The problem has never been the Gricean approach as such, but rather to find the right 'alternatives'.

In the present theory:

- The maxims are sensitive to attentive content
- Attentive content mirrors sub-sentential structure.
- (Hence so do the 'alternatives'.)


## 4.3. 'Embedded' implicatures

Chierchia, et al. (2008), and much subsequent discussion
(6) Which books (among O. and K.L.) did every student read? Every student read O. or K.L. $\leadsto$ No student read both.

The problem
The problem has never been the Gricean approach as such, but rather to find the right 'alternatives'.

In the present theory:

- The maxims are sensitive to attentive content
- Attentive content mirrors sub-sentential structure.
- (Hence so do the 'alternatives'.)

The 'embedded' implicature of (6) is in fact predicted.

### 4.4. Other suitable semantics

Attentive semantics is not the only suitable semantics:

### 4.4. Other suitable semantics

Attentive semantics is not the only suitable semantics:

- Unrestricted Inquisitive Sem. (Ciardelli, 2009; Westera, 2012)


### 4.4. Other suitable semantics

Attentive semantics is not the only suitable semantics:

- Unrestricted Inquisitive Sem. (Ciardelli, 2009; Westera, 2012)

Minimally, the semantics must lack the absorption laws:

- Absorption: $p \vee(p \wedge q) \equiv p \equiv p \wedge(p \vee q)$


### 4.4. Other suitable semantics

Attentive semantics is not the only suitable semantics:

- Unrestricted Inquisitive Sem. (Ciardelli, 2009; Westera, 2012)

Minimally, the semantics must lack the absorption laws:

- Absorption: $p \vee(p \wedge q) \equiv p \equiv p \wedge(p \vee q)$



### 4.5. Roberts's (1996) 'relevance'

- 'My' Maxim of Relation: $R_{s} \vDash Q$
- Roberts's relevance: $R_{C G} \vDash Q \quad(C G=$ Common Ground)


### 4.5. Roberts's (1996) 'relevance'

- 'My' Maxim of Relation: $R_{s} \vDash Q$
- Roberts's relevance: $R_{C G} \vDash Q \quad(C G=$ Common Ground)

Roberts's requirement is too strong:

### 4.5. Roberts's (1996) 'relevance'

- 'My' Maxim of Relation: $R_{s} \vDash Q$
- Roberts's relevance: $R_{C G} \vDash Q \quad(C G=$ Common Ground)

Roberts's requirement is too strong:

- The participants need not already know how $R$ is relevant.


### 4.5. Roberts's (1996) 'relevance'

- 'My' Maxim of Relation: $R_{s} \vDash Q$
- Roberts's relevance: $R_{C G} \vDash Q \quad(C G=$ Common Ground)

Roberts's requirement is too strong:

- The participants need not already know how $R$ is relevant.
- They need only be able to figure it out.


### 4.5. Roberts's (1996) 'relevance'

- 'My' Maxim of Relation: $R_{s} \vDash Q$
- Roberts's relevance: $R_{C G} \vDash Q$
(CG $=$ Common Ground)

Roberts's requirement is too strong:

- The participants need not already know how $R$ is relevant.
- They need only be able to figure it out.
E.g., in case of exhaustivity:

1. $s \subseteq|p|$
2. $s \nsubseteq|q|$
3. $s \subseteq \overline{|p|} \cup|q|$ or $s \subseteq \overline{|p|} \cup \overline{|q|}$
4. $s \subseteq \overline{|q|}$

### 4.6. One-sided/two-sided numerals

(7) a. There are three apples.
b. There are at least three apples.
c. There are exactly three apples.

### 4.6. One-sided/two-sided numerals

(7) a. There are three apples.
b. There are at least three apples.
c. There are exactly three apples.

Does (7a) mean (7b) ('one-sided') or (7c) ('two-sided')?

### 4.6. One-sided/two-sided numerals

(7) a. There are three apples.
b. There are at least three apples.
c. There are exactly three apples.

Does (7a) mean (7b) ('one-sided') or (7c) ('two-sided')?

### 4.6. One-sided/two-sided numerals

(7) a. There are three apples.
b. There are at least three apples.
c. There are exactly three apples.
$\exists x \cdot A x \wedge|x|=3$
$\exists x \cdot A x \wedge|x| \geq 3$
$\exists!x \cdot A x \wedge|x|=3$

Does (7a) mean (7b) ('one-sided') or (7c) ('two-sided')?

### 4.6. One-sided/two-sided numerals

(7) a. There are three apples.
b. There are at least three apples.
c. There are exactly three apples.

$$
\begin{array}{r}
\exists x \cdot A x \wedge|x|=3 \\
\exists x \cdot A x \wedge|x| \geq 3 \\
\exists!x \cdot A x \wedge|x|=3
\end{array}
$$

Does (Ta) mean (7b) ('one-sided') or (7c) ('two-sided')? Neither!


### 4.6. One-sided/two-sided numerals

(7) a. There are three apples.
b. There are at least three apples.
c. There are exactly three apples.

$$
\begin{array}{r}
\exists x \cdot A x \wedge|x|=3 \\
\exists x \cdot A x \wedge|x| \geq 3 \\
\exists!x \cdot A x \wedge|x|=3
\end{array}
$$

Does (7a) mean (7b) ('one-sided') or (7c) ('two-sided')? Neither!
(7a) (0) (1) (3) (4) (6)
(7b) (0) (1) (3) (5) 6

### 4.6. One-sided/two-sided numerals

(7) a. There are three apples.
b. There are at least three apples.
c. There are exactly three apples.

$$
\begin{array}{r}
\exists x \cdot A x \wedge|x|=3 \\
\exists x \cdot A x \wedge|x| \geq 3 \\
\exists!x \cdot A x \wedge|x|=3
\end{array}
$$

Does (7a) mean (7b) ('one-sided') or (7c) ('two-sided')? Neither!
(7a) (0) (1) (3) (4) (5)
(7b) (0) (1) (3) (4) 6
(7c) (0) (1) (2) (5) (6)

### 4.6. One-sided/two-sided numerals

(cf. Coppock and Brochhagen, 2013)
(7) a. There are three apples.
b. There are at least three apples.
c. There are exactly three apples.

$$
\begin{array}{r}
\exists x \cdot A x \wedge|x|=3 \\
\exists x \cdot A x \wedge|x| \geq 3 \\
\exists!x \cdot A x \wedge|x|=3
\end{array}
$$

Does (7a) mean (7b) ('one-sided') or (7c) ('two-sided')? Neither!
(7a) (0) (1) (3) (4) (6)
(7b) (0) (1) (3) (4) 6
(7c) (0) (1) (2) (4) (5)

## Fin.

## Contact <br> Matthijs Westera - m.westera@uva.nl

## Article

- Attentive Pragmatics: Exhaustivity and the Final Rise. ESSLLI StuS proceedings (staff.science.uva.nl/~westera/)

Thanks to the Netherlands Organisation for Scientific Research (NWO) for financial support; to F. Roelofsen, J. Groenendijk, the audiences of SemDial (Paris), S-Circle (UC Santa Cruz), SPE6 (St Petersburg) and many anonymous reviewers for valuable comments.

## Appendix A. Semantics (Roelofsen, 2011)

Ingredients

- Possibility: a set of worlds $(a, b)$
- Proposition: a set of possibilities $(A, B,[\varphi])$
- Informative content: $|\varphi|:=\bigcup[\varphi]$
- $A$ restricted to $b, A_{b}:=\{a \cap b \mid a \in A, a \cap b \neq \varnothing\}$

Semantics of relevant fragment

1. $[p]=\{\{w \in$ Worlds $\mid w(p)=$ true $\}\}$
2. $[\varphi \vee \psi]=([\varphi] \cup[\psi])_{|\varphi| \cup|\psi|}=[\varphi] \cup[\psi]$
3. $[\varphi \wedge \psi]=([\varphi] \cup[\psi])_{|\varphi| \cap|\psi|}$

## Entailment

$A$ entails $B, A \vDash B$, iff (i) $\cup A \subseteq \cup B$ and (ii) $B_{\cup A} \subseteq A$.

## Appendix B. The final rise

To be presented at ESSLLI.
(7) Which colours (among red, green and blue) does John like? He likes blue $\pi$.

## Appendix B. The final rise

To be presented at ESSLLI.
(7) Which colours (among red, green and blue) does John like? He likes blue $\pi$.

Conveys uncertainty regarding:

- whether he really likes blue


## Appendix B. The final rise

To be presented at ESSLLI.
(7) Which colours (among red, green and blue) does John like? He likes blue $\pi$.

Conveys uncertainty regarding:

- whether he really likes blue
- whether this is sufficient info


## Appendix B. The final rise

To be presented at ESSLLI.
(7) Which colours (among red, green and blue) does John like? He likes blue $\nearrow$.

Conveys uncertainty regarding:

- whether he really likes blue
- whether this is sufficient info
- whether 'blue' is pronounced correctly


## Appendix B. The final rise

To be presented at ESSLLI.
(7) Which colours (among red, green and blue) does John like? He likes blue $\pi$.

Conveys uncertainty regarding:

- whether he really likes blue
- whether this is sufficient info
- whether 'blue' is pronounced correctly
- whether he likes red


## Appendix B. The final rise

To be presented at ESSLLI.
(7) Which colours (among red, green and blue) does John like? He likes blue $\pi$.

Conveys uncertainty regarding:

- whether he really likes blue
- whether this is sufficient info
- whether 'blue' is pronounced correctly
- whether he likes red

Proposal
The final rise conveys uncertain cooperativity.

## Appendix B. The final rise

To be presented at ESSLLI.
(7) Which colours (among red, green and blue) does John like? He likes blue $\nearrow$.

Conveys uncertainty regarding:

- whether he really likes blue
(Quality)
- whether this is sufficient info
- whether 'blue' is pronounced correctly
- whether he likes red

Proposal
The final rise conveys uncertain cooperativity.

## Appendix B. The final rise

To be presented at ESSLLI.
(7) Which colours (among red, green and blue) does John like? He likes blue $\nearrow$.

Conveys uncertainty regarding:

- whether he really likes blue
(Quality)
- whether this is sufficient info
- whether 'blue' is pronounced correctly
- whether he likes red

Proposal
The final rise conveys uncertain cooperativity.

## Appendix B. The final rise

To be presented at ESSLLI.
(7) Which colours (among red, green and blue) does John like? He likes blue $\pi$.

Conveys uncertainty regarding:

- whether he really likes blue
(Quality)
- whether this is sufficient info
- whether 'blue' is pronounced correctly
(Quantity)
(Manner)
- whether he likes red

Proposal
The final rise conveys uncertain cooperativity.

## Appendix B. The final rise

To be presented at ESSLLI.
(7) Which colours (among red, green and blue) does John like? He likes blue $\pi$.

Conveys uncertainty regarding:

- whether he really likes blue
(Quality)
- whether this is sufficient info
- whether 'blue' is pronounced correctly
- whether he likes red
(Quantity)
(Manner)
(Relation)

Proposal
The final rise conveys uncertain cooperativity.

## Appendix C. References

- Chierchia, G., Fox, D., \& Spector, B. (2008). The grammatical view of scalar implicatures and the relationship between semantics and pragmatics.
- Ciardelli, I. (2009). Inquisitive semantics and intermediate logics.
- Coppock, E., \& Brochhagen, T. (2013). Raising and resolving issues with scalar modifiers.
- Gazdar (1979): Pragmatics: Implicature, Presupposition, and Logical Form.
- Grice, H. (1975). Logic and conversation.
- Groenendijk, J., \& Stokhof, M. (1984). Studies on the semantics of questions and the pragmatics of answers.
- Roberts, C. (1996). Information structure in discourse.
- Roelofsen, F. (2011). Information and attention.
- Sauerland, U. (2004). Scalar implicatures in complex sentences.
- Westera, M. (2012). Meanings as proposals: a new semantic foundation for Gricean pragmatics.

